

# A Unified Online-Offline Framework for Co-Branding Campaign Recommendations

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# Introduction

- Cobranding represents a powerful marketing strategy.
- Involve two brands collaborating to create a unique product or campaign.
- Enhance market reach, brand equity, and appeal to diverse demographics.
- Example:
  - Making luxury accessible (Versace + H&M),
  - Elevating premium design (BlackBerry + Porsche Design),
  - Or targeting niche lifestyles (Nike + Apple)
- Cobranding drives innovation and strengthens consumer connections.

## CO-BRANDING

1

 **VERSACE** +  = 

*MORE AFFORDABILITY / WIDER ACCESSIBILITY  
for Versace products in H&M stores*

2

 +  = 

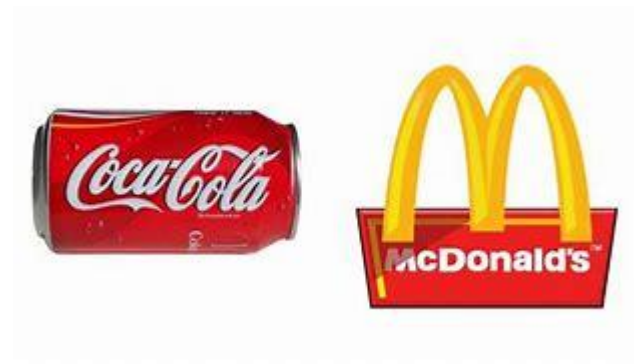
*HIGHER PREMIUM ON BLACKBERRY  
since it attaches itself to the Porsche Design  
brand equity*

3

 +  = 

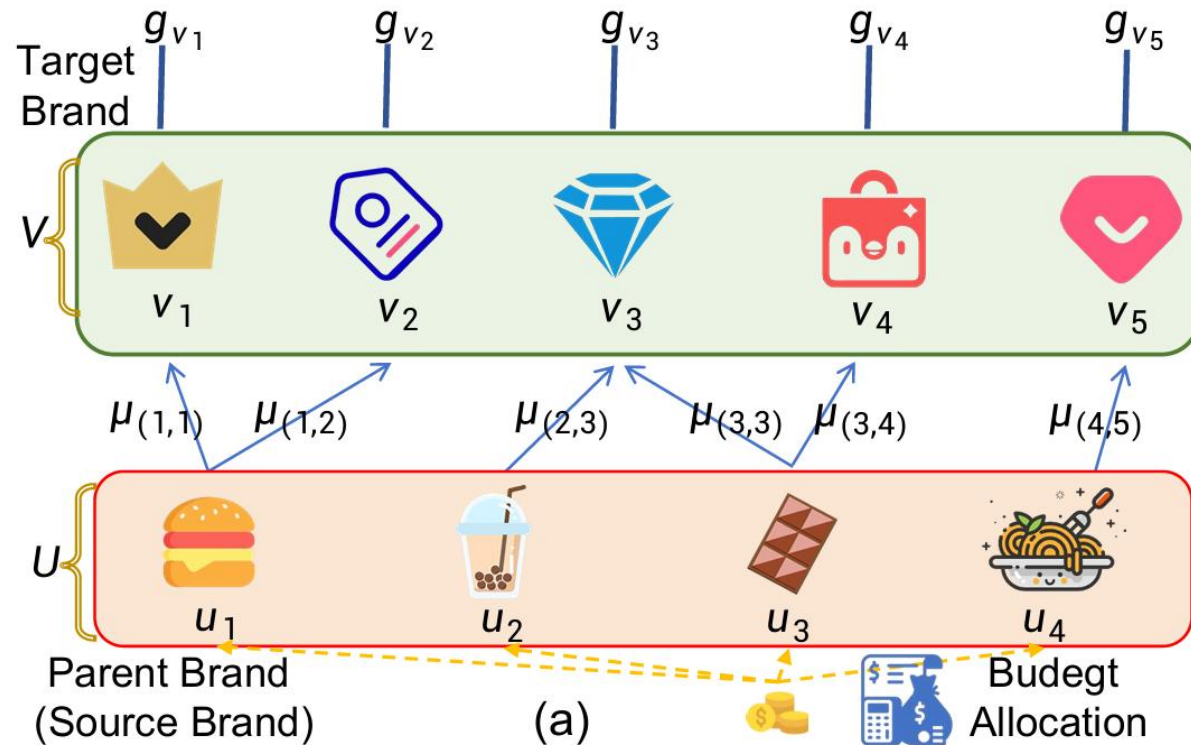
*APPEAL TO A NICHE MARKET/ CERTAIN LIFESTYLE  
a wider demographic is reached Nike appealing  
to Apple users and vice versa*

# Introduction



- **Partner Selection:** Mismatched collaborations can reduce profits or harm reputation.
- **Market Uncertainty:** Unpredictable factors like the **Matthew Effect**, consumer fatigue, and shifting preferences create risks.
- **Partner Willingness:** Target brands' participation is uncertain due to **brand positioning** and **financial commitment**.
- **Exploration Exploitation:** Balancing known partnerships with new ones is tricky, given **high costs** and **early risks**.
- **Budget Constraints:** Managing **multiple subbrands** requires holistic budget allocation for maximum **collective benefits**.

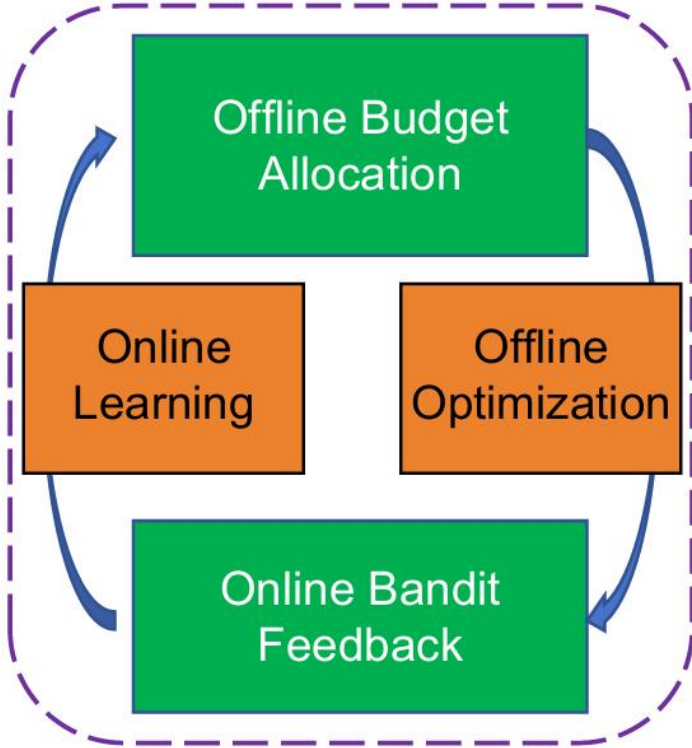
# Model



## CoBranding Bipartite Graph Model

- $\mathcal{G} = (\mathcal{U}, \mathcal{V}, \mathcal{E})$  models cobranding opportunities between a parent brand and potential partner brands.
- $\mathcal{U}$  : Subbrands  $|\mathcal{U}| = U$  from parent brand system.
- $\mathcal{V}$  : Target partner brands  $|\mathcal{V}| = V$ .
- Edges  $e := (u, v) \in \mathcal{E}$  : Represent cobranding pairs.
- Weight vector  $\boldsymbol{\mu} = \{\mu_e\}_{e \in \mathcal{E}}$  : Probability of success, influenced by alignment and budget.
- Market gain vector  $\mathbf{g} = \{g_v\}_{v \in \mathcal{V}}$  : Revenue from target brand  $v$  to entire parent brand company  $\mathcal{U}$ .
- Visual: See Figure right  $U=4, V=5$ .

# Problem Formulation



## Unified Problem Formulation

- **$\alpha$ -approximate regret:**

$$Reg(T) = \alpha T \cdot r_{\mathcal{G}}(\mathbf{b}^*) - \mathbb{E} \left[ \sum_{t=1}^T r_{\mathcal{G}}(\mathbf{b}_t^A) \right], \quad (4)$$

- Objective: Minimize  $Reg(T)$  for optimal longterm strategy.

## Online Feedback Mechanism

- T round (co-branding season) online learning process.
- Budget allocation:  $\mathbf{b}_t = (b_{t,1}, \dots, b_{t,U})$  per season.
- Action:  $S_t^{\mathbf{b}_t} \subseteq \mathcal{E}$  for cobranding pairings.
- Feedback:  $\mathbf{X}_{t,S_t} = (X_{t,1}, \dots, X_{t,|S_t|}) \in [0, 1]^{|S_t|}$  (success propensity) and  $\mathbf{Y}_{t,\mathcal{V}}$  (market gain) observed.
- Reward:  $R_{\mathcal{G}}(\mathbf{b}_t) = \sum_{v \in \mathcal{V}} \mathbb{I}\{\exists e = (u, v) \in S_t \text{ s.t. } X_{t,e,b_u} = 1\} Y_{t,v}, \quad (1)$
- Goal: Learn **probability of successful co-branding** and **brand market gain** to maximize cumulative reward.

## Offline Strategic Budget Allocation

- Total budget  $B$  allocated as  $\mathbf{b} = (b_1, \dots, b_U)$ .
- Constraints: Each subbrand is assigned a predetermined budget cap.
- Expected reward:  $r_{\mathcal{G}}(\mathbf{b}) = \sum_{v \in \mathcal{V}} g_v \left( 1 - \prod_{e=(u,v) \in S} (1 - \mu_{e,b_u}) \right).$  (2)
- Optimization: Maximize expected reward under constraints, **NP-hard**, solved via  **$\alpha$ -approximation**.
- Goal: Prioritize highpotential subbrands within budget limits.



# Algorithm

## Algorithmic Workflow

Hybrid online-offline: Integrate online and offline processes for co-branding optimization.

- ① Estimate co-branding bipartite graph  $G$ .
- ② Allocate budget to select optimal co-branding pairs.
- ③ Execute initial campaigns and collect market feedback.
- ④ Refine graph estimates with feedback.
- ⑤ Re-optimize for subsequent campaigns.



**Overview:** Combines dynamic learning with strategic planning for maximum market impact.

# Algorithm

## Graph Learning via Online Feedback

### Exploration-Exploitation Trade-off:

- ◆ Co-branding bipartite information often partially or unknown.
- ◆ Naive best-partner selection risks local optima.
- ◆ Solution: Confidence-based Multi-Armed Bandit (MAB) strategy.

### Enhancements:

- ◆ Bernstein-type bound tightens confidence radius using variance.
- ◆ Non-decreasing UCBs reflect realistic spending trends.
- ◆ Historical data initializes but excludes from radius for short-term focus.

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### Algorithm 1 Confidence-Based Online Learning for Co-Branding (CBOL)

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**Require:** Set of co-branding initiators  $\mathcal{U}$ , set of target brands  $\mathcal{V}$ .

- 1: Initialize  $T_{t,e,s}$ ,  $\hat{\mu}_{e,s}$  for each  $(e, s) \in \mathcal{A}$ , and  $T'_v$ ,  $\hat{g}_v$  for each  $v \in \mathcal{A}'$  using historical dataset  $\mathcal{D}$ .
  - 2: **for** season  $t = 0, 1, 2, \dots, T$  **do**
  - 3:   For  $(e, s) \in \mathcal{A}$ ,  $\rho_{e,s} \leftarrow \text{Eq. (5)}$ ,  $\tilde{\mu}_{e,s} \leftarrow \hat{\mu}_{e,s} + \rho_{e,s}$ ,  $\bar{\mu}_{e,s} \leftarrow \max_{j \in N_u, j \leq s} \tilde{\mu}_{e,j}$ .
  - 4:   For  $v \in \mathcal{A}'$ ,  $\rho'_v \leftarrow \sqrt{\frac{6\hat{V}_v \log t}{T_{t,v}}} + \frac{9 \log t}{T_{t,v}}$ ,  $\hat{g}_v \leftarrow \hat{g}_v + \rho'_v$ .
  - 5:   Budget allocation  $\mathbf{b} \leftarrow \text{GPE (Algorithm 2)}$ .
  - 6:   Observe co-branding intention feedback  $X_{t,S_t}$  under budget allocation  $\mathbf{b}$ .
  - 7:   For each  $(e, s)$  that receives feedback  $X_{e,s}$ , update  $T_{t,e,s} \leftarrow T_{t,e,s} + 1$ ,  $\hat{\mu}_{e,s} \leftarrow \hat{\mu}_{e,s} + (X_{e,s} - \hat{\mu}_{e,s})/T_{t,e,s}$ ,  $\hat{V}_{e,s} \leftarrow \frac{T_{t,e,s}-1}{T_{t,e,s}} \left( \hat{V}_{e,s} + \frac{1}{T_{t,e,s}} (\hat{\mu}_{e,s} - X_{t,e,s})^2 \right)$ .
  - 8:   For any successful co-branding pair  $e \in S_t$  with  $X_{t,e,s} = 1$ , observe market gain  $Y_{t,\mathcal{V}}$  and update  $T'_{t,v} \leftarrow T'_{t,v} + 1$ ,  $\hat{g}_v \leftarrow \hat{g}_v + (Y_v - \hat{g}_v)/T'_{t,v}$ ,  $\hat{V}'_v \leftarrow \frac{T'_{t,v}-1}{T'_{t,v}} \left( \hat{V}'_v + \frac{1}{T'_{t,v}} (\hat{g}_v - Y_{t,v})^2 \right)$ .
  - 9: **end for**
-

# Algorithm

## Budget Optimization via Offline Planning

### Submodular Property Basis:

- ◆ Reward exhibits **diminishing marginal returns**.
- ◆ **Total** marginal gain decreases as budget shifts to one sub-brand.

### Refining Approximation Ratio:

- ◆ Improves on  $\alpha$  with **partial enumeration**.
- ◆ Focuses on **quality over time complexity** due to high co-branding costs.

### Integration with Online Learning:

- ◆ Use **learned bipartite graph** for campaign execution.
- ◆ Balance budget planning **across multiple partners** or proportionally.
- ◆ Feedback **updates estimates** for future seasons.

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## Algorithm 2 Greedy Partial Enumeration for Budget Optimization (GPE)

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**Require:** Co-Branding graph  $\mathcal{G}$ , total budget  $B$ , budget cap  $c_u$ , tentative spending plans  $\mathcal{N}_u, u \in \mathcal{U}$ , operational constraint  $K$ .

- 1: Initialize  $b_{max} \leftarrow 0$ .
  - 2:  $\mathcal{B} \leftarrow \{b = (b_1, \dots, b_U) \mid 0 \leq b_u \leq c_u, b_u \in \mathcal{N}_u, \sum_{u \in \mathcal{U}} b_u \leq B, \sum_{u \in \mathcal{U}} \mathbb{I}\{b_u > 0\} \leq K\}$ .
  - 3: **for**  $b \in \mathcal{B}$  **do**
  - 4:    $B' \leftarrow B - \sum_{u \in \mathcal{U}} b_u$ .
  - 5:   Let  $Q \leftarrow \{(u, s_u) \mid u \in \mathcal{U}, s_u \in \mathcal{N}_u, 1 \leq s_u \leq c_u - b_u\}$ .
  - 6:   **while**  $B' > 0$  and  $Q \neq \emptyset$  **do**
  - 7:      $(u^*, s^*) \leftarrow \arg \max_{(u,s) \in Q} \delta(u, s, b) / s$ .
  - 8:     **if**  $s^* \leq B'$  **then**
  - 9:        $s_{u^*} \leftarrow s_{u^*} + s^*, B' \leftarrow B' - s^*$ .
  - 10:       Adjust all pairs  $(u^*, s) \in Q$  to  $(u^*, s - s^*)$ .
  - 11:       Remove all pairs  $(u^*, s) \in Q$  such that  $s \leq 0$ .
  - 12:     **else**
  - 13:       Remove  $(u^*, s^*)$  from  $Q$ .
  - 14:     **end if**
  - 15:   **end while**
  - 16:   **if**  $r_{\mathcal{G}}(b) > r_{\mathcal{G}}(b_{max})$ , **then**  $b_{max} \leftarrow b$ .
  - 17: **end for**
-



# Theoretical Analysis

## Online Learning

- **Regret Bound (Theorem 1):** Algorithm 1 achieves  $O(V \sqrt{(NU + 1)T \log T} + \log(UVT + VT) \log T)$  sub-linear regret.
- **Remark 1:**
  - ◆ Expand base arms from  $\mathcal{A}$  to  $\mathcal{A} \cup \mathcal{A}'$  for unknown market gains.
  - ◆ Redefine the definition of the set of triggered arms in previous works, improving the leading term by  $O((U + 1)/(NU + 1))$ .
  - ◆ Use historical data average to bound regret with a constant.

## Offline Optimization

- **Approximation (Theorem 2):** Algorithm 2 achieves  $(1 - 1/e)$ -approximate solution (i.e.,  $\alpha = 1 - 1/e$ ).
- **Remark 2:**
  - ◆ Combines partial enumeration and greedy methods.
  - ◆ Best polynomial-time solution unless  $P=NP$ .
  - ◆ Time complexity:  $O(BN^2UV^2)$  of any partial enumeration, scales linearly with  $U$ , quadratically with  $V$ .
  - ◆ Practical efficiency with finite allocation plans (e.g., 3 tiers: low, medium, high).
  - ◆  $K=3$  balance time and performance.

# Experiment

## Research Questions

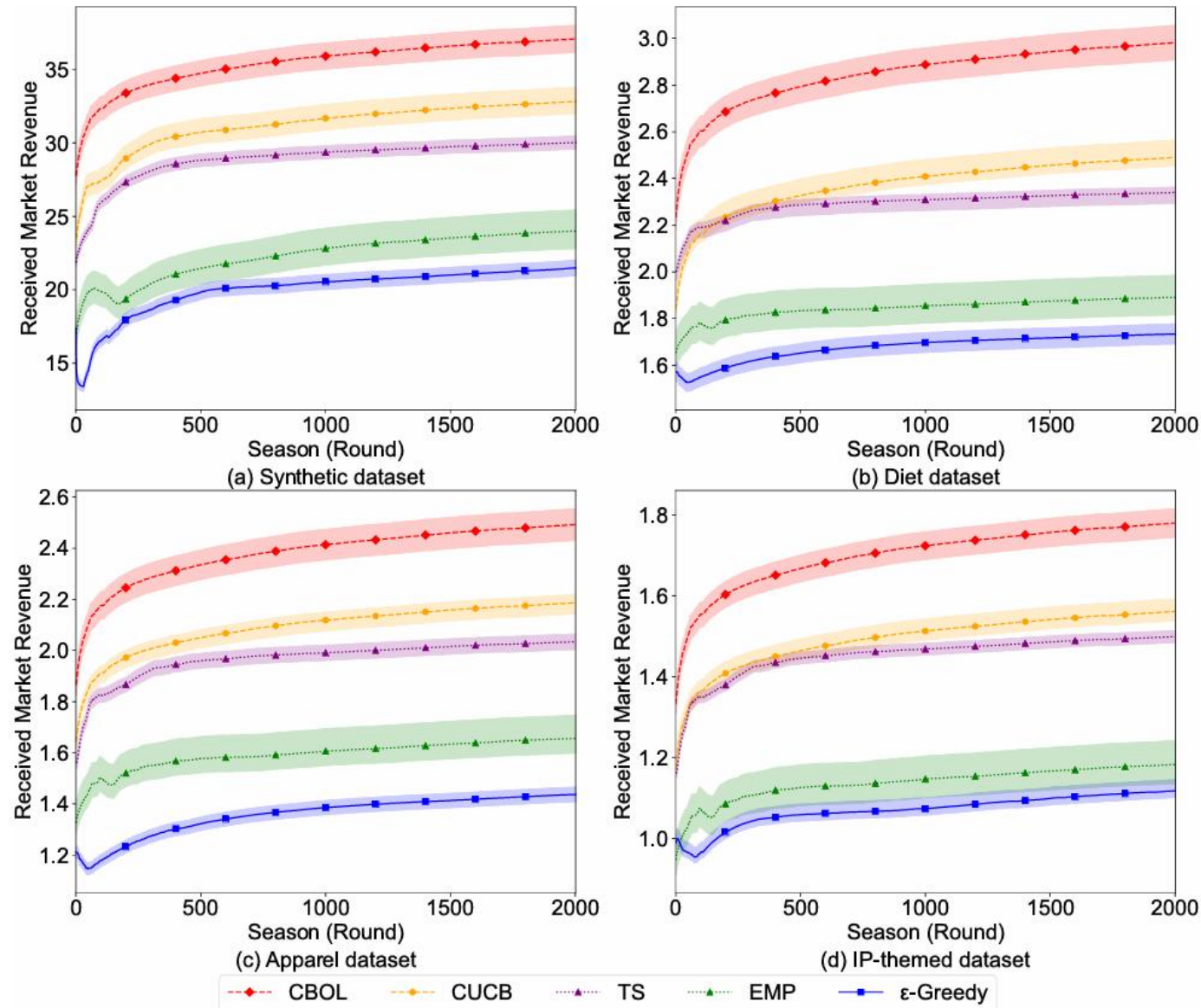
- **RQ1:** Can online learning algorithm outperform in high-uncertainty co-branding for shortand long-term revenue?
- **RQ2:** Does offline budget strategy enhance revenue across multiple sub-brands?
- **RQ3:** Is framework stable across varying budgets, seasons, and plans?

## Real-world Datasets.

- 3,500 cases from SocialBeta and dataworld:
- Datasets: Diet (269  $U$ , 608  $V$ ), Apparel (192  $U$ , 471  $V$ ), IP-themed (161  $U$ , 405  $V$ ).

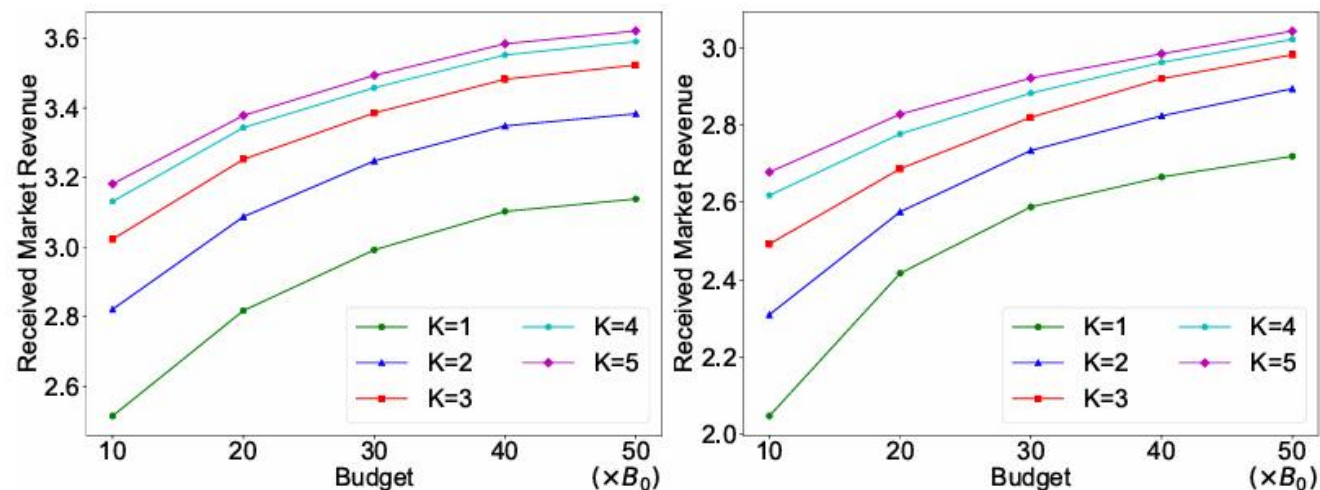
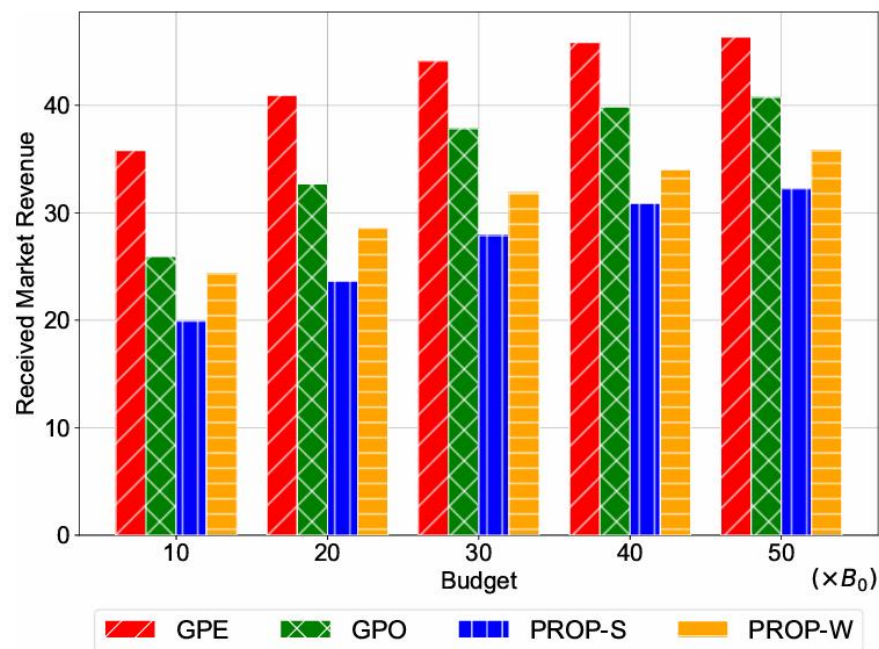
## Evaluation Results

- **Co-branding Online Performance (RQ1):** Outperforms baselines by 12%-73%, fastest convergence on market revenue.

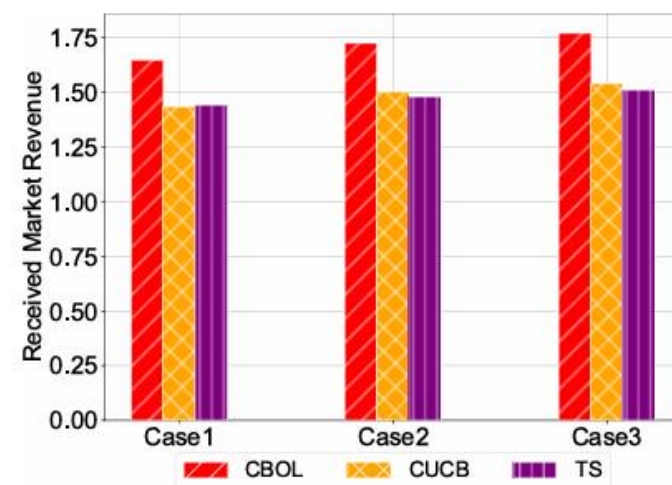
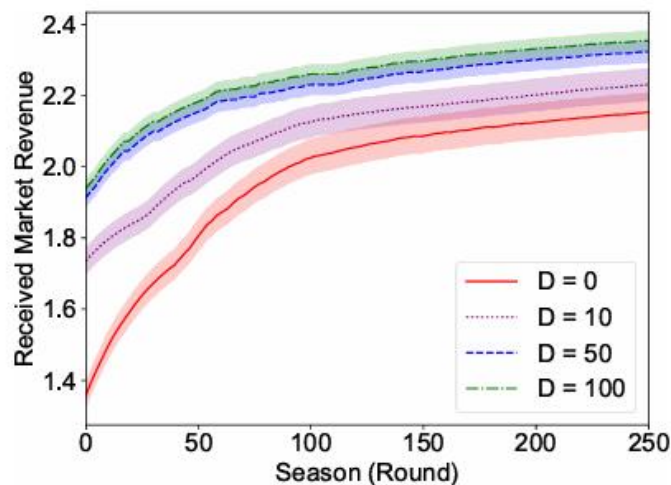


# Experiment

- **Offline Budget Allocation (RQ2):** Improve revenue from holistic parent brand perspective.
- **Performance-Cost Tradeoff (RQ2 & RQ3):** Revenue rises with  $K=1$  to 3, marginal beyond 4; Running time:  $K=4,5$  significantly increase.
- **Impact of Historical Dataset (RQ1):** Boost early performance, mitigate unnecessary exploration loss.
- **Ablation Study (RQ3):** Consistently best.



Value of $K$	1	2	3	4	5
Average running time (s)	0.1304	0.3214	0.8921	1.9052	3.5116
Average reward	2.9126	3.1772	3.3329	3.4148	3.4515
Increase of running time	0	146.1%	584.0%	1361.6%	2592.7%



Thank You :)